

Try This 1 Solutions

TT 1. *Foundations and Pre-calculus Mathematics 10* (Pearson)

- a. *Foundations and Pre-calculus Mathematics 10* (Pearson), “Exercises” questions 5, 8, 15 and 20 on pages 233 and 234

5. Since $2^{10} = 1024$, $2^{-10} = \frac{1}{1024}$.

8. a) $3^{-2} = \frac{1}{3^2}$
 $= \frac{1}{9}$

8. b) $2^{-4} = \frac{1}{2^4}$
 $= \frac{1}{16}$

8. c) $(-2)^{-5} = \frac{1}{(-2)^5}$
 $= -\frac{1}{32}$

8. d) $\left(\frac{1}{3}\right)^{-3} = \left(\frac{3}{1}\right)^3$
 $= 27$

8. e) $\left(-\frac{2}{3}\right)^{-2} = \left(-\frac{3}{2}\right)^2$
 $= \left(-\frac{3}{2}\right)\left(-\frac{3}{2}\right)$
 $= \frac{9}{4}$

8. f) $\frac{1}{5^{-3}} = 5^3$
 $= 125$

15. $I = 100d^{-2}$
 $= 100(23)^{-2}$
 $= \frac{100}{23^2}$
 $\doteq 0.1890359168\%$

The intensity of light 23 cm from the source would be 0.19%.

- 20.** If a number is raised to a negative exponent, it will not always be less than 1. Some cases where a number raised to a negative exponent is greater than or equal to 1 are as follows:

- If a positive fraction less than 1 or a positive decimal less than 1 is raised to a negative exponent, the value of the power will be greater than 1.

$$\left(\frac{1}{3}\right)^{-3} = \left(\frac{3}{1}\right)^3 \\ = 27$$

- If a negative fraction less than 1 or a negative decimal less than 1 is raised to a negative even exponent, it will be greater than 1.

$$\left(-\frac{1}{2}\right)^{-4} = \left(-\frac{2}{1}\right)^4 \\ = 16$$

- If the number 1 is raised to any negative exponent, the result will always be 1.

$$1^{-3} = \frac{1}{1^3} \\ = 1$$

- If the number -1 is raised to an even negative exponent, the result will always be 1.

$$(-1)^{-4} = \frac{1}{(-1)^4} \\ = \frac{1}{1} \\ = 1$$

- b.** *Foundations and Pre-calculus Mathematics 10* (Pearson), “Exercises” questions 4.b, 4.d, 7.b, 7.c, 8, 9, and 11.b, and d on pages 241 and 242

4. b) $0.5^2 \times 0.5^3 = 0.5^{2+3}$
 $= 0.5^5$

$$\begin{aligned} 4. \quad \mathbf{d)} \quad \frac{0.5^2}{0.5^{-3}} &= 0.5^{2-(-3)} \\ &= 0.5^5 \end{aligned}$$

$$\begin{aligned} 7. \quad \mathbf{b)} \quad \left[\left(\frac{3}{5} \right)^3 \right]^{-4} &= \left(\frac{3}{5} \right)^{(3)(-4)} \\ &= \left(\frac{3}{5} \right)^{-12} \\ &= \left(\frac{5}{3} \right)^{12} \end{aligned}$$

$$\begin{aligned} 7. \quad \mathbf{c)} \quad \left[\left(\frac{3}{5} \right)^{-3} \right]^{-4} &= \left(\frac{3}{5} \right)^{(-3)(-4)} \\ &= \left(\frac{3}{5} \right)^{12} \end{aligned}$$

$$8. \quad \mathbf{a)} \quad \left(\frac{a}{b} \right)^2 = \frac{a^2}{b^2}$$

$$\begin{aligned} 8. \quad \mathbf{b)} \quad \left(\frac{n^2}{m} \right)^3 &= \frac{n^{2(3)}}{m^3} \\ &= \frac{n^6}{m^3} \end{aligned}$$

$$\begin{aligned} 8. \quad \mathbf{c)} \quad \left(\frac{c^2}{d^2} \right)^{-4} &= \left(\frac{d^2}{c^2} \right)^4 \\ &= \frac{d^{2(4)}}{c^2(4)} \\ &= \frac{d^8}{c^8} \end{aligned}$$

$$\begin{aligned} 8. \quad \mathbf{d)} \quad \left(\frac{2b}{5c} \right)^2 &= \frac{2^2 b^2}{5^2 c^2} \\ &= \frac{4b^2}{25c^2} \end{aligned}$$

8. e) $(ab)^2 = a^2b^2$

8. f) $(n^2m)^3 = n^{(2)(3)}m^3$
 $= n^6m^3$

8. g) $(c^3d^2)^{-4} = c^{(3)(-4)}d^{(2)(-4)}$
 $= c^{-12}d^{-8}$
 $= \frac{1}{c^{12}d^8}$

8. h) $(xy^{-1})^{-3} = x^{(-3)}y^{(-1)(-3)}$
 $= x^{-3}y^3$
 $= \frac{y^3}{x^3}$

9. a) Use the product law: When the bases are the same, add the exponents.

$$x^{-3}x^4 = x^{-3+4}$$

$$= x^1$$

9. b) Use the product law: When the bases are the same, add the exponents.

$$a^{-4}a^{-1} = a^{-4+(-1)}$$

$$= a^{-5}$$

Then write with positive exponents.

$$a^{-5} = \frac{1}{a^5}$$

9. c) Use the product law: When the bases are the same, add the exponents.

$$b^4b^{-3}b^2 = b^{4-3+2}$$

$$= b^3$$

9. d) Use the product law: When the bases are the same, add the exponents.

$$\begin{aligned}
 m^8 m^{-2} m^{-6} &= m^{8 + (-2) + (-6)} \\
 &= m^0 \\
 &= 1
 \end{aligned}$$

9. e) Use the quotient law: When the bases are the same, subtract the exponents.

$$\begin{aligned}
 \frac{x^{-5}}{x^2} &= x^{-5-(2)} \\
 &= x^{-7}
 \end{aligned}$$

Then write with positive exponents.

$$x^{-7} = \frac{1}{x^7}$$

9. f) Use the quotient law: When the bases are the same, subtract the exponents.

$$\begin{aligned}
 \frac{s^5}{s^{-5}} &= s^{5-(-5)} \\
 &= s^{10}
 \end{aligned}$$

9. g) Use the quotient law: When the bases are the same, subtract the exponents.

$$\begin{aligned}
 \frac{b^{-8}}{b^{-3}} &= b^{-8-(-3)} \\
 &= b^{-5}
 \end{aligned}$$

Then write with positive exponents.

$$b^{-5} = \frac{1}{b^5}$$

9. h) Use the quotient law: When the bases are the same, subtract the exponents.

$$\begin{aligned}
 \frac{t^{-4}}{t^{-4}} &= t^{-4-(-4)} \\
 &= t^0 \\
 &= 1
 \end{aligned}$$

11. b) Use the power of a power law: For each power, multiply the exponents.

$$\begin{aligned}\left(2a^{-2}b^2\right)^{-2} &= 2^{-2}a^{(-2)(-2)}b^{(2)(-2)} \\ &= 2^{-2}a^4b^{-4}\end{aligned}$$

Then write with positive exponents.

$$\begin{aligned}2^{-2}a^4b^{-4} &= \frac{a^4}{2^2b^4} \\ &= \frac{a^4}{4b^4}\end{aligned}$$

$$\begin{aligned}11. \text{ d) } \left(\frac{3}{2}m^{-2}n^{-3}\right)^{-4} &= \left(\frac{3}{2}\right)^{-4}m^8n^{12} \\ &= \left(\frac{2}{3}\right)^4m^8n^{12} \\ &= \frac{2^4}{3^4}m^8n^{12} \\ &= \frac{16}{81}m^8n^{12}\end{aligned}$$

or

11. d) Use the power of a power law: For each power, multiply the exponents.

$$\begin{aligned}\left(\frac{3}{2}m^{-2}n^{-3}\right)^{-4} &= \left(\frac{3}{2}\right)^{-4}m^{(-2)(-4)}n^{(-3)(-4)} \\ &= \left(\frac{2}{3}\right)^4m^8n^{12} \\ &= \frac{16m^8n^{12}}{81}\end{aligned}$$