

- If you have any difficulty with these solutions, please contact your teacher before continuing.

Page 357, *Your Turn*

a.

Write both sides of the equation as powers of 4.

$$4^{x+5} = 64^{2x}$$

$$4^{x+5} = (4^3)^{2x}$$

$$4^{x+5} = 4^{6x}$$

$$x + 5 = 6x$$

$$5 = 5x$$

$$1 = x$$

Verify the answer by substituting $x = 1$ into the original equation.

Left Side	Right Side
4^{x+5}	64^{2x}
4^{1+5}	$64^{2(1)}$
4^6	64^2
4096	4096

Because the left side is equal to the right side, the answer $x = 1$ is verified to be correct.Page 362, *Question 7*

b. $8(3)^{\frac{x}{2}} = 72$

$$(3)^{\frac{x}{2}} = \frac{72}{8}$$

$$(3)^{\frac{x}{2}} = 9$$

$$(3)^{\frac{x}{2}} = 3^2$$

$$\frac{x}{2} = 2$$

$$x = 4$$

e. $4^{1-2x} = 32$

$$(2^2)^{1-2x} = 2^5$$

$$2^{2-4x} = 2^5$$

$$2 - 4x = 5$$

$$-4x = 3$$

$$x = -\frac{3}{4}$$

f. $10^{2(x-3)} = 1000$

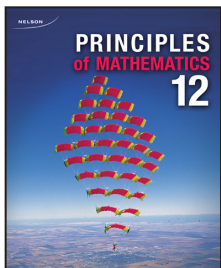
$$10^{2(x-3)} = 10^3$$

$$2(x-3) = 3$$

$$2x - 6 = 3$$

$$2x = 9$$

$$x = 4.5$$



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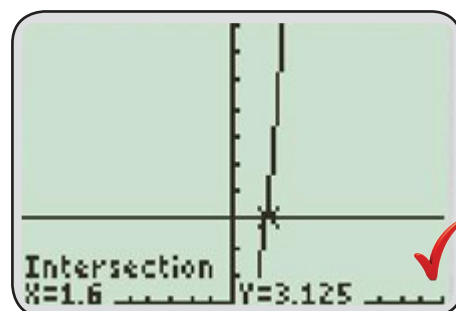
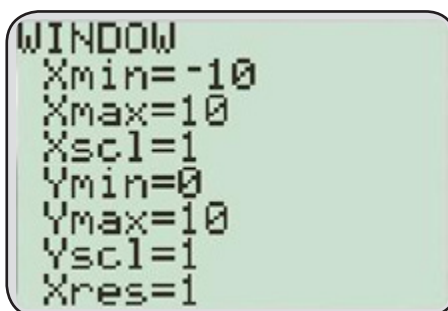
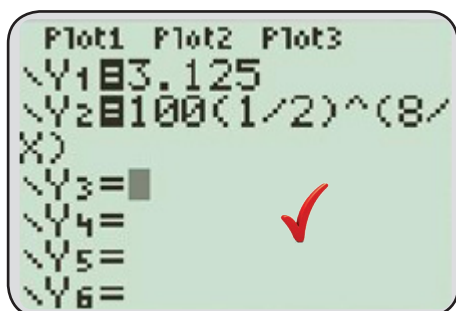
Page 359, *Your Turn*

- a. Substitute the values $A_0 = 100$, $A(x) = 3.125$, and $x = 8$ into the half-life equation.

$$A(x) = A_0 \left(\frac{1}{2} \right)^{\frac{x}{h}}$$

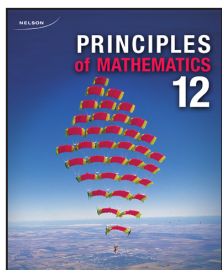
$$3.125 = 100 \left(\frac{1}{2} \right)^{\frac{8}{h}} \quad \checkmark$$

Graph the terms on each side of the equation and find the intersection points.



The solution to the equation is the x -value of the intersection point, $x = 1.6$.

When the divers are at 1.6 m below the surface, the visibility will be half the visibility at the surface. ✓



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Page 363, Question 10

If the original amount $A_0 = 100$ then, half the original amount means $A(t) = 50$.

a. $A(t) = A_0 \left(\frac{1}{2} \right)^{\frac{t}{5.3}}$

$$50 = 100 \left(\frac{1}{2} \right)^{\frac{t}{5.3}} \quad \checkmark$$

$$\frac{50}{100} = \left(\frac{1}{2} \right)^{\frac{t}{5.3}}$$

$$\frac{1}{2} = \left(\frac{1}{2} \right)^{\frac{t}{5.3}} \quad \checkmark$$

$$\left(\frac{1}{2} \right)^1 = \left(\frac{1}{2} \right)^{\frac{t}{5.3}}$$

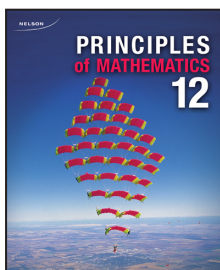
$$1 = \frac{t}{5.3} \quad \checkmark$$

$$5.3 = t$$

It takes 5.3 years for cobalt-60 to reduce to half its original amount. \checkmark

b. $A(t) = A_0 \left(\frac{1}{2} \right)^{\frac{t}{5.3}} = 100 \left(\frac{1}{2} \right)^{\frac{10}{5.3}} \cong 27 \quad \checkmark$

After ten years, approximately 27% of cobalt-60 will remain. \checkmark



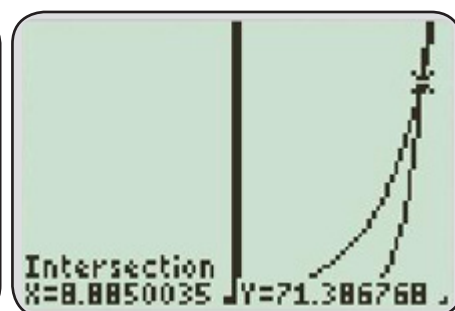
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Page 360, *Your Turn*

- Graph the terms on each side of the equation and find the intersection points.

```
Plot1 Plot2 Plot3
\Y1=3^(X-5)
\Y2=2(5)^(X/4)
\Y3=
\Y4=
\Y5=
\Y6=
\Y7=
```

```
WINDOW
Xmin=-10
Xmax=10
Xscl=1
Ymin=0
Ymax=90
Yscl=1
Xres=1
```



The solution to the equation is the x -value of the intersection point, $x \approx 8.885$.

The solution, to one decimal place, is $x = 8.9$.

Page 364, *Question 14*

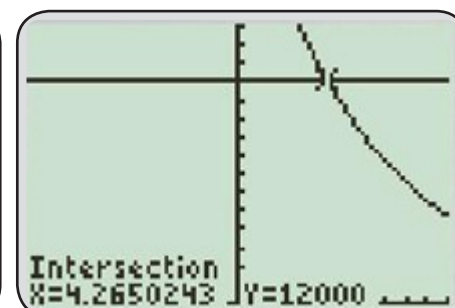
- Substitute the value $V(t) = 12\,000$ into the equation.

$$V(t) = 24\,000(0.85)^t$$

$$12\,000 = 24\,000(0.85)^t$$

```
Plot1 Plot2 Plot3
\Y1=12000
\Y2=24000(0.85)^X
\Y3=
\Y4=
\Y5=
\Y6=
```

```
WINDOW
Xmin=-10
Xmax=10
Xscl=1
Ymin=0
Ymax=15000
Yscl=1000
Xres=1
```



The solution to the equation is the x -value of the intersection point, $x \approx 4.265$.

The vehicle will be worth \$12 000 about 4.27 years after the purchase date.