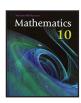


Enhance Your Understanding

Lesson 7.1: Slope-Intercept Form of a Linear Equation



Refer to page 349 in *Mathematics 10* for more practice.

Page 349, #1a, 1c, 1e, 2, 3c, 3d, 5a, 5c, 5e, 6b, 6f, 7, 8, 9a, 10d, and 13

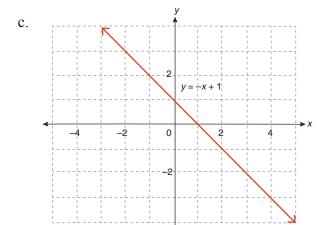
Question 1, page 349

- a. The slope is -5 and the y-intercept is 4.
- c. The slope is 1 and the y-intercept is -7.
- e. This equation can be written as y = 0x 3, so the slope is 0 and the y-intercept is -3.

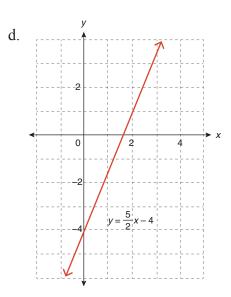
Question 2, page 349

- a. The slope is -3 and the *y*-intercept is 2.
- b. To sketch the graph of this line, start by plotting the *y*-intercept, (0, 2), on the graph. From this point, move 3 units down and 1 unit right and mark the point (1, -1). Connect the points using a straight edge.

Question 3, page 349



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Question 5, page 350

a.
$$2x + y = 6$$
$$2x - 2x + y = 6 - 2x$$
$$y = -2x + 6$$

The slope is -2 and the *y*-intercept is 6.

c.
$$5x + 6y = 8$$

 $5x - 5x + 6y = 8 - 5x$
 $6y = 8 - 5x$
 $\frac{6y}{6} = \frac{8 - 5x}{6}$
 $y = \frac{8}{6} - \frac{5x}{6}$
 $y = \frac{4}{3} - \frac{5x}{6}$
 $y = -\frac{5}{6}x + \frac{4}{3}$

The slope is $-\frac{5}{6}$ and the *y*-intercept is $\frac{4}{3}$.

e.
$$7x - y + 9 = 0$$

 $7x - \cancel{y} + \cancel{y} + 9 = 0 + y$
 $7x + 9 = y$

The slope is 7 and the *y*-intercept is 9.

Question 6, page 350

b.
$$m = \frac{5}{6}, b = -4$$
$$y = mx + b$$
$$y = \frac{5}{6}x - 4$$

f.
$$m = 0, b = \frac{1}{3}$$
$$y = mx + b$$
$$y = 0x + \frac{1}{3}$$
$$y = \frac{1}{3}$$

Question 7, page 350

- a. Since the slopes of equations A and C are positive, these lines slope up from left to right.
- b. Since the slopes of equations B and D are negative, these lines slope down from left to right.
- c. Equation C has the greatest y-intercept, followed by B, then D, then A.
- d. Since the *y*-intercept for equation D is (0, 0), Line D is the only one that passes through the origin.

Question 8, page 351

a.
$$m = 4, b = 4$$
$$y = mx + b$$
$$y = 4x + 4$$

b.
$$m = -\frac{1}{2}, b = -1$$

 $y = mx + b$
 $y = -\frac{1}{2}x - 1$

c.
$$m = -2, b = 6$$

 $y = mx + b$
 $y = -2x + 6$

d.
$$m = \frac{2}{3}, b = 4$$
$$y = mx + b$$
$$y = \frac{2}{3}x + 4$$

e.
$$m = 0, b = -2.5$$

 $y = mx + b$
 $y = 0x - 2.5$
 $y = -2.5$

f.
$$m = \frac{2}{5}, b = 4$$
$$y = mx + b$$
$$y = \frac{2}{5}x + 4$$

Question 9, page 351

a. To find the value of b, substitute the coordinates of the point (4, 9) into the equation y = 3x + b.

$$9 = 3(4) + b$$

$$9 = 12 + b$$

$$9 - 12 = 1/2 - 1/2 + b$$
$$-3 = b$$

Question 10, page 351

d. To find the value of m, substitute the coordinates of the point (-6, -1) into the equation y = mx - 2.

$$-1 = m(-6) - 2$$

$$-1 = -6m - 2$$

$$-1 + 2 = -6m - 2 + 2$$

$$1 = -6m$$

$$\frac{1}{-6} = \frac{-6m}{-6}$$

$$-\frac{1}{6} = m$$

Question 13, page 353

a.
$$C = 300 + 6.25n$$

b.
$$T = 3.60 + 1.48x$$

c.
$$D = 1024 + 54t$$

d.
$$L = 2500 - 120t$$

Lesson 7.2: General Form of a Linear Equation



Refer to page 365 in Mathematics 10 for more practice.

Page 365, #1, 2a, 2d, 3c, 3g, 4, 5, 6, 8, 11, and 14

Question 1, page 365

When Jasmine multiplied both sides of the equation by 2, she missed multiplying the constant 4 by 2.

$$y = -\frac{3}{2}x + 4$$

$$(2)y = 2\left(-\frac{3}{2}x\right) + 2(4)$$

$$2y = -3x + 8$$

$$3x + 2y - 8 = 0$$

Question 2, page 365

a.
$$y = 7x - 5$$

 $\cancel{y} - \cancel{y} = 7x - 5 - y$
 $0 = 7x - y - 5$

d.
$$y = -\frac{3}{5}x - 2$$
$$y + \frac{3}{5}x + 2 = -\frac{3}{5}x - 2 + \frac{3}{5}x + 2$$
$$\frac{3}{5}x + y + 2 = 0$$
$$5(\frac{3}{5}x + y + 2) = 5(0)$$
$$3x + 5y + 10 = 0$$

Question 3, page 365

c. The x-intercept occurs where y = 0, so substitute 0 for y and solve for x.

$$x-2y+10 = 0$$

$$x-2(0)+10 = 0$$

$$x+10 = 0$$

$$x+10-10 = 0-10$$

$$x = -10$$

The x-intercept occurs at (-10, 0).

The y-intercept occurs where x = 0, so substitute 0 for x and solve for y.

$$x - 2y + 10 = 0$$

$$0 - 2y + 10 = 0$$

$$-2y + 10 = 0$$

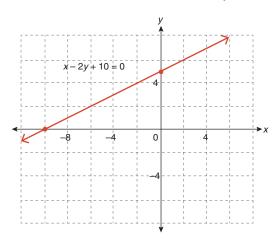
$$-2y + 10 - 10 = 0 - 10$$

$$-2y = -10$$

$$\frac{-2y}{-2} = \frac{-10}{-2}$$

$$y = 5$$

The y-intercept occurs at (0, 5).



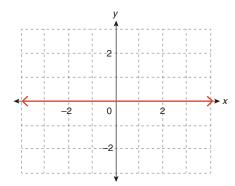
Unit 7: Equations and Graphs of Linear Relations

g. The x-intercept occurs where y = 0, so substitute 0 for y.

$$0 = 0$$

There are an infinite number of *x*-intercepts.

The y-intercept occurs where x = 0. This occurs at (0,0) since y is always zero.



Question 4, page 365

a. Domain: $\{x | x \in R\}$

Range:
$$\{y | y = 2\}$$

There is no x-intercept and the y-intercept occurs at (0,2).

The slope is 0.

$$y - 2 = 0$$

b. Domain: $\{x | x = -3\}$

Range:
$$\{y | y \in R\}$$

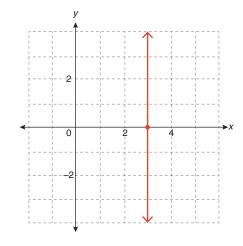
The *x*-intercept occurs at (-3,0) and there is no *y*-intercept.

The slope is undefined.

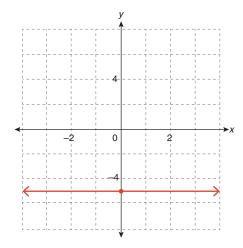
$$x + 3 = 0$$

Question 5, page 366

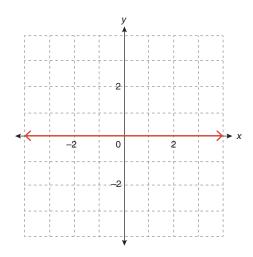
a. x - 3 = 0



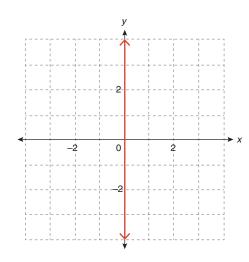
b.
$$y + 5 = 0$$



c.
$$y = 0$$



d.
$$x = 0$$



Unit 7: Equations and Graphs of Linear Relations

Question 6, page 366

a.
$$3x + 4y = 12$$

 $3x - 3x + 4y = 12 - 3x$
 $4y = -3x + 12$
 $\frac{4y}{4} = \frac{-3x + 12}{4}$
 $y = -\frac{3}{4}x + \frac{12}{4}$
 $y = -\frac{3}{4}x + 3$

Line 2 is the only line with a slope of $-\frac{3}{4}$ and a *y*-intercept of 3.

b.
$$x = 4$$

Line 4 is the only vertical line with an *x*-intercept of 4.

c.
$$3x - 4y = 12$$

 $3x - 3x - 4y = 12 - 3x$
 $-4y = -3x + 12$
 $\frac{-4y}{-4} = \frac{-3x + 12}{-4}$
 $y = \frac{\cancel{-}3}{\cancel{-}4}x + \frac{12}{-4}$
 $y = \frac{3}{4}x - 3$

Line 8 is the only line with a slope of $\frac{3}{4}$ and a *y*-intercept of -3.

d.
$$y-3=0$$
$$y-3 + 3 = 0 + 3$$
$$y = 3$$

Line 5 is the only horizontal line with a *y*-intercept of 3.

e.
$$3x - 4y + 12 = 0$$
$$3x - 4y + 12 - 3x - 12 = 0 - 3x - 12$$
$$-4y = -3x - 12$$
$$\frac{-4y}{-4} = \frac{-3x - 12}{-4}$$
$$y = \frac{-3x}{-4} - \frac{12}{-4}$$
$$y = \frac{3}{4}x + 3$$

Line 3 is the only line with a slope of $\frac{3}{4}$ and a *y*-intercept of 3.

f.
$$y = -3$$

Line 6 is the only horizontal line with a y-intercept of -3.

g.
$$3x + 4y + 12 = 0$$
$$3x + 4y + 12 - 3x - 12 = 0 - 3x - 12$$
$$4y = -3x - 12$$
$$\frac{4y}{4} = \frac{-3x - 12}{4}$$
$$y = \frac{-3x}{4} - \frac{12}{4}$$
$$y = -\frac{3}{4}x - 3$$

Line 7 is the only line with a slope of $-\frac{3}{4}$ and a *y*-intercept of -3.

h.
$$x + 4 = 0$$

 $x = -4$

Line 1 is the only vertical line with an x-intercept of -4.

Question 8, page 366

If a line does not have a *y*-intercept, then it is a vertical line. This vertical line passes through the point (3,6).

$$x = 3$$

$$x - 3 = 3 - 3$$

$$x - 3 = 0$$

Question 11, page 367

- a. 8x + 11y = 440, where x represents the number of minutes Luc swims the backstroke and y represents the number of minutes he swims the butterfly.
- b. The x-intercept occurs where y = 0, so substitute 0 for y and solve for x.

$$8x + 11y = 440$$

$$8x + 11(0) = 440$$

$$8x = 440$$

$$\frac{8x}{8} = \frac{440}{8}$$

$$x = 55$$

The y-intercept occurs where x = 0, so substitute 0 for x and solve for y.

$$8x + 11y = 440$$

$$8(0) + 11y = 440$$

$$11y = 440$$

$$\cancel{1/y} = \frac{440}{11}$$

$$y = 40$$

The *x*-intercept of 55 represents the number of minutes Luc must swim the backstroke to burn 440 calories (without swimming the butterfly). The *y*-intercept of 40 represents the number of minutes Luc must swim the butterfly to burn 440 calories (without swimming the backstroke).

c.
$$8x + 11y = 440$$
$$8x + 11(16) = 440$$
$$8x + 176 = 440$$
$$8x + 176 - 176 = 440 - 176$$
$$8x = 264$$
$$\frac{8x}{8} = \frac{264}{8}$$
$$x = 33$$

Luc must swim the backstroke for 33 minutes.

Question 14, page 368

a.
$$Ax + 5y - 6 = 0$$

$$A(-3) + 5(2) - 6 = 0$$

$$-3A + 10 - 6 = 0$$

$$-3A + 4 = 0$$

$$-3A + 4 - 4 = 0 - 4$$

$$-3A = -4$$

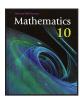
$$\frac{\cancel{3}A}{\cancel{3}} = \frac{-4}{-3}$$

$$A = \frac{4}{3}$$

b.
$$2x + By + 7 = 0$$
$$2(4) + B(5) + 7 = 0$$
$$8 + 5B + 7 = 0$$
$$5B + 15 = 0$$
$$5B + 15 = 0 - 15$$
$$5B = -15$$
$$\frac{5B}{5} = \frac{-15}{5}$$
$$B = -3$$

c.
$$4x - 3y + C = 0$$
$$4(-2) - 3(-6) + C = 0$$
$$-8 + 18 + C = 0$$
$$10 + C = 0$$
$$C + 10 - 10 = 0 - 10$$
$$C = -10$$

Lesson 7.3: Slope Point Form of a Linear Equation



Refer to page 377 in Mathematics 10 for more practice.

Page 377, #1f, 2a, 2b, 3a, 4, 6a, 7, 10, 13, and 14

Question 1, page 377

f. slope-intercept form

$$y+9 = -\frac{2}{3}(x-6)$$

$$y+9 = -\frac{2}{3}x + \frac{12}{3}$$

$$y+9 = -\frac{2}{3}x + 4$$

$$y+9-9 = -\frac{2}{3}x + 4 - 9$$

$$y = -\frac{2}{3}x - 5$$

general form

$$y = -\frac{2}{3}x - 5$$

$$y + \frac{2}{3}x + 5 = -\frac{2}{3}x - 5 + \frac{2}{3}x + 5$$

$$y + \frac{2}{3}x + 5 = 0$$

$$3(\frac{2}{3}x + y + 5) = 3(0)$$

$$2x + 3y + 15 = 0$$

Question 2, page 377

a.
$$y - y_1 = m(x - x_1)$$

 $y - 2 = 2(x - 3)$

b.
$$y-y_1 = m(x-x_1)$$

 $y-(-3) = -\frac{3}{2}(x-1)$
 $y+3 = -\frac{3}{2}(x-1)$

Question 3, page 377

a.
$$y - y_1 = m(x - x_1)$$
$$y - (-2) = 6(x - 5)$$
$$y + 2 = 6(x - 5)$$
$$y + 2 = 6x - 30$$
$$y + 2 - 2 = 6x - 30 - 2$$
$$y = 6x - 32$$
$$0 = 6x - y - 32$$

Question 4, page 377

- a. The slope is $\frac{2}{3}$ and (6, 1) is a point on the line.
- b. Plot the point (6,1). From the point (6,1), go up 2 units (rise) and go 3 units to the right (run) to find a second point. Draw the line passing through the two points.

Question 6, page 378

a.
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{-7 - 1}{3 - 5}$$

$$= \frac{-8}{-2}$$

$$= 4$$

Use the point (5, 1) to write the equation.

$$y - y_1 = m(x - x_1)$$

$$y - 1 = 4(x - 5)$$

$$y - 1 = 4x - 20$$

$$y - 1 + 1 = 4x - 20 + 1$$

$$y = 4x - 19$$

$$0 = 4x - y - 19$$

Question 7, page 378

- a. Compare the graphs of the equations using slope-point form, or rewrite the equations in slope-intercept form and compare the equations.
- b. Convert all equations to slope-intercept form and compare.

①
$$y-2=3(x+1)$$
 ③ $y+5=3(x+1)$
 $y-2=3x+3$ $y+5=3x+3$
 $y-2+2=3x+3+2$ $y+5-5=3x+3-5$
 $y=3x+5$ $y=3x-2$

②
$$y-10 = 3(x-4)$$
 ④ $y-11 = 3(x-2)$
 $y-10 = 3x-12$ $y-11 = 3x-6$
 $y-10 + 10 = 3x-12 + 10$ $y-11 + 11 = 3x-6 + 11$
 $y=3x-2$ $y=3x+5$

Equations 1 and 4 represent the same line, and equations 2 and 3 represent the same line.

Unit 7: Equations and Graphs of Linear Relations

Question 10, page 379

a.
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
$$= \frac{7 - 1}{3 - 0}$$
$$= \frac{6}{3}$$
$$= 2$$

$$y = mx + b$$
$$1 = 2(0) + b$$
$$1 = b$$

The equation of the line is y = 2x + 1.

b.
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

= $\frac{7 - 1}{3 - 0}$
= $\frac{6}{3}$
= 2

$$y - y_1 = m(x - x_1)$$

 $y - 1 = 2(x - 0)$
 $y - 1 = 2x$

The equation of the line is y - 1 = 2x.

c. The equations represent the same graph.

Question 13, page 379

a.
$$V - V_1 = m(t - t_1)$$

 $V - 29 = 1.2(t - 24)$

The equation V - 29 = 1.2(t - 24) gives the volume of oil in the tank at time t.

b.
$$V-29 = 1.2(t-24)$$

$$155-29 = 1.2(t-24)$$

$$126+28.8 = 1.2t-28.8 + 28.8$$

$$154.8 = 1.2t$$

$$\frac{154.8}{1.2} = \frac{1.2t}{1.2}$$

$$129 = t$$

It will take 129 hours to fill the tank.

c.
$$V-29 = 1.2(t-24)$$

$$V-29 = 1.2(0-24)$$

$$V-29 = 0-28.8$$

$$V-29 + 28.8 = 0-28.8 + 28.8$$

$$V-0.2 = 0$$

$$V = 0.2$$

No. The tank contained 0.2 m³ of oil prior to filling.

Question 14, page 380

a.
$$m = \frac{V_2 - V_1}{t_2 - t_1}$$
$$= \frac{341 - 335}{16 - 6}$$
$$= \frac{6}{10}$$
$$= \frac{3}{5}$$

The slope of the line is $\frac{3}{5}$.

b. The slope represents a rate of change of 0.6 m/s per $^{\circ}\text{C}$.

c.
$$V - V_1 = m(t - t_1)$$

 $V - 335 = \frac{3}{5}(t - 6)$

d.
$$V-335 = \frac{3}{5}(35-6)$$
$$V-335 = 21-3.6$$
$$V-335 + 335 = 17.4 + 335$$
$$V = 352.4$$

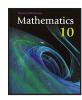
The velocity of sound at an air temperature of 35°C is 352.4 m/s.

e.
$$348 - 335 = \frac{3}{5}(t - 6)$$

 $13 = \frac{3}{5}t - 3.6$
 $13 + 3.6 = \frac{3}{5}t - 3.6 + 3.6$
 $16.6 = \frac{3}{5}t$
 $5(16.6) = 5(\frac{3}{5}t)$
 $83 = 3t$
 $\frac{83}{3} = \frac{5}{3}t$
 $27.666... = t$

For the velocity of sound to be 348 m/s, the air temperature must be about 28°C.

Lesson 7.4: Parallel and Perpendicular Lines



Refer to page 390 in Mathematics 10 for more practice.

Page 390, #1a, 1c, 1e, 1g, 2a, 2c, 3, 4a, 5a, 5c, 5e, 6a, 7a, 9, 11, and 17

Question 1, page 390

- a. The slope of a parallel line is 5. The slope of a perpendicular line is $-\frac{1}{5}$.
- c. The slope of a parallel line is $-\frac{1}{3}$. The slope of a perpendicular line is 3.
- e. The slope of a parallel line is 0.5. The slope of a perpendicular line is -2.
- g. The slope of a parallel line is 0. The slope of a perpendicular line is undefined.

Question 2, page 391

a. The slope of the line $y = \frac{3}{7}x + 4$ is $\frac{3}{7}$. The slope of a parallel line is $\frac{3}{7}$ and the slope of a perpendicular line is $-\frac{7}{3}$.

c.
$$3x + y - 5 = 0$$

$$3x + y - 5 - 3x + 5 = 0 - 3x + 5$$

 $y = -3x + 5$

The slope of the line 3x + y - 5 = 0 is -3. The slope of a parallel line is -3 and the slope of a perpendicular line is $\frac{1}{3}$.

Question 3, page 391

a.
$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
$$= \frac{1 - 9}{-2 - (-6)}$$
$$= \frac{-8}{4}$$
$$= -2$$

The slope of a parallel line would be -2.

b. The slope of a perpendicular line is the negative reciprocal of -2, which is $\frac{1}{2}$.

Question 4, page 391

a. To be parallel, the lines must have equal slopes.

$$\frac{n}{10} = \frac{2}{1}$$

$$\frac{n}{10}(10) = \frac{2}{1}(10)$$

$$n = 20$$

To be perpendicular, the slopes must have a product of -1.

$$\left(\frac{n}{10}\right)\left(\frac{2}{1}\right) = -1$$

$$\frac{2n}{10} = -1$$

$$\frac{2n}{10}(10) = -1(10)$$

$$2n = -10$$

$$\frac{2n}{2} = \frac{-10}{2}$$

$$n = -5$$

Question 5, page 391

- a. Neither; the slopes are neither equal, nor negative reciprocals.
- c. Parallel; the slopes are equal.

$$y_1 = -x + 8$$

$$y_2 = -x + 2$$

e. Neither; the slopes are neither equal, nor negative reciprocals.

$$5x + 2y - 10 = 0$$
$$2y = -5x + 10$$
$$y = -\frac{5}{2}x + 5$$

$$2x + 5y + 10 = 0$$
$$5y = -2x - 10$$
$$y = -\frac{2}{5}x - 2$$

Question 6, page 391

a. The slope of the original line is 2, so the parallel line must also have a slope of 2.

$$y = mx + b$$

$$y = 2x + b$$

$$-6 = 2(1) + b$$

$$-6 = 2 + b$$

$$-6-2 = \cancel{2} - \cancel{2} + b$$

$$-8 = b$$

$$y = 2x - 8$$

Question 7, page 392

a. The slope of the original line is 3. The negative reciprocal of 3 is $-\frac{1}{3}$, so the slope of the new line is $-\frac{1}{3}$.

$$y = mx + b$$

$$5 = -\frac{1}{3}(9) + b$$

$$5 = -3 + b$$

$$5 + 3 = \sqrt{3} + b + 3$$

$$8 = b$$

$$y = -\frac{1}{3}x + 8$$

Question 9, page 392

Compare the slopes of sides AB and DC as well as sides AD and BC. If these pairs of slopes are equal, then the shape is a parallelogram.

Find the slope of segment *AB*:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
$$= \frac{3 - 5}{3 - (-4)}$$
$$= \frac{-2}{7}$$

Find the slope of segment *DC*:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$
$$= \frac{-3 - (-1)}{5 - (-2)}$$
$$= \frac{-2}{7}$$

Find the slope of segment *AD*:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{5 - (-1)}{-4 - (-2)}$$

$$= \frac{6}{-2}$$

$$= -3$$

Find the slope of segment *BC*:

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{3 - (-3)}{3 - 5}$$

$$= \frac{6}{-2}$$

$$= -3$$

Since the two pairs of slopes are equal, the opposite sides are parallel and the quadrilateral is a parallelogram.

Question 11, page 392

a.
$$m_2 = \frac{y_2 - y_1}{x_2 - x_1}$$

 $m_2 = \frac{5 - 3}{1 - 4}$
 $= -\frac{2}{3}$

The slope of Line 2 is $-\frac{2}{3}$. This means Line 1 must also have a slope of $-\frac{2}{3}$ to be parallel to Line 2.

$$m_{1} = \frac{y_{2} - y_{1}}{x_{2} - x_{1}}$$

$$\frac{2}{-3} = \frac{4 - (-2)}{n - 1}$$

$$\frac{2}{-3} = \frac{6}{n - 1}$$

$$(n - 1)\frac{2}{-3} = \frac{6}{n - 1}(n - 1)$$

$$\frac{(n - 1)2}{-3} = 6$$

$$(-3)\frac{(n - 1)2}{-3} = 6(-3)$$

$$2n - 2 = -18$$

$$2n - 2 + 2 = -18 + 2$$

$$2n = -16$$

$$\frac{2n}{2} = \frac{-16}{2}$$

$$n = -8$$

b. The slope of Line 2 is $-\frac{2}{3}$. The slope of Line 1 must be the negative reciprocal of $-\frac{2}{3}$ for the lines to be perpendicular. So, the slope of Line 1 must be $\frac{3}{2}$.

$$m_{2} = \frac{y_{2} - y_{1}}{x_{2} - x_{1}}$$

$$\frac{3}{2} = \frac{4 - (-2)}{n - 1}$$

$$\frac{3}{2} = \frac{6}{n - 1}$$

$$(n - 1)\frac{3}{2} = \frac{6}{n - 1}$$

$$\frac{(n - 1)3}{2} = 6$$

$$(2)\frac{(n - 1)3}{2} = 6(2)$$

$$3n - 3 = 12$$

$$3n - 3 + 3 = 12 + 3$$

$$3n = 15$$

$$\frac{3n}{3} = \frac{15}{3}$$

$$3n = 5$$

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$$H = 0.7(220 - A)$$

$$H = 154 - 0.7A$$

$$H = -0.7A + 154$$

$$H = 0.8(220 - A)$$

$$H = 176 - 0.8A$$

$$H = -0.8A + 176$$

The slopes of H = 0.7(220 - A) and H = 0.8(220 - A) are -0.7 and -0.8, respectively. Since the slopes are not equal, these equations do not represent parallel lines.